



National
Qualifications
2018

X747/76/11

**Mathematics
Paper 1 (Non-Calculator)**

THURSDAY, 3 MAY
9:00 AM – 10:10 AM

Total marks — 60

Attempt ALL questions.

You may NOT use a calculator.

Full credit will be given only to solutions which contain appropriate working.

State the units for your answer where appropriate.

Answers obtained by readings from scale drawings will not receive any credit.

Write your answers clearly in the spaces provided in the answer booklet. The size of the space provided for an answer should not be taken as an indication of how much to write. It is not necessary to use all the space.

Additional space for answers is provided at the end of the answer booklet. If you use this space **you must clearly identify the question number** you are attempting.

Use **blue** or **black** ink.

Before leaving the examination room you must give your answer booklet to the Invigilator; if you do not, you may lose all the marks for this paper.



FORMULAE LIST

Circle:

The equation $x^2 + y^2 + 2gx + 2fy + c = 0$ represents a circle centre $(-g, -f)$ and radius $\sqrt{g^2 + f^2 - c}$.

The equation $(x - a)^2 + (y - b)^2 = r^2$ represents a circle centre (a, b) and radius r .

Scalar Product:

$\mathbf{a} \cdot \mathbf{b} = |\mathbf{a}| |\mathbf{b}| \cos \theta$, where θ is the angle between $\mathbf{a}$ and $\mathbf{b}$

or $\mathbf{a} \cdot \mathbf{b} = a_1 b_1 + a_2 b_2 + a_3 b_3$ where $\mathbf{a} = \begin{pmatrix} a_1 \\ a_2 \\ a_3 \end{pmatrix}$ and $\mathbf{b} = \begin{pmatrix} b_1 \\ b_2 \\ b_3 \end{pmatrix}$.

Trigonometric formulae:

$$\sin(A \pm B) = \sin A \cos B \pm \cos A \sin B$$

$$\cos(A \pm B) = \cos A \cos B \mp \sin A \sin B$$

$$\sin 2A = 2 \sin A \cos A$$

$$\cos 2A = \cos^2 A - \sin^2 A$$

$$= 2 \cos^2 A - 1$$

$$= 1 - 2 \sin^2 A$$

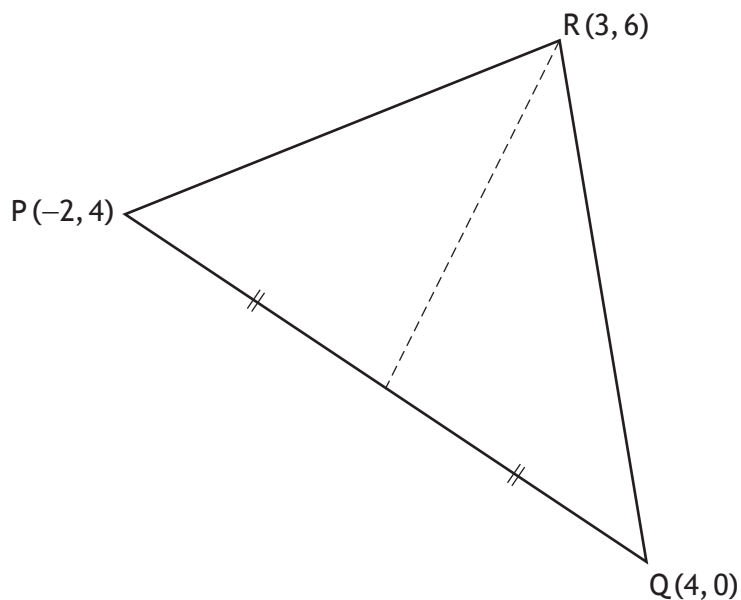
Table of standard derivatives:

$f(x)$	$f'(x)$
$\sin ax$	$a \cos ax$
$\cos ax$	$-a \sin ax$

Table of standard integrals:

$f(x)$	$\int f(x) dx$
$\sin ax$	$-\frac{1}{a} \cos ax + c$
$\cos ax$	$\frac{1}{a} \sin ax + c$

1. PQR is a triangle with vertices $P(-2, 4)$, $Q(4, 0)$ and $R(3, 6)$.



Find the equation of the median through R .

3

2. A function $g(x)$ is defined on $\mathbb{R}$, the set of real numbers, by

$$g(x) = \frac{1}{5}x - 4.$$

Find the inverse function, $g^{-1}(x)$.

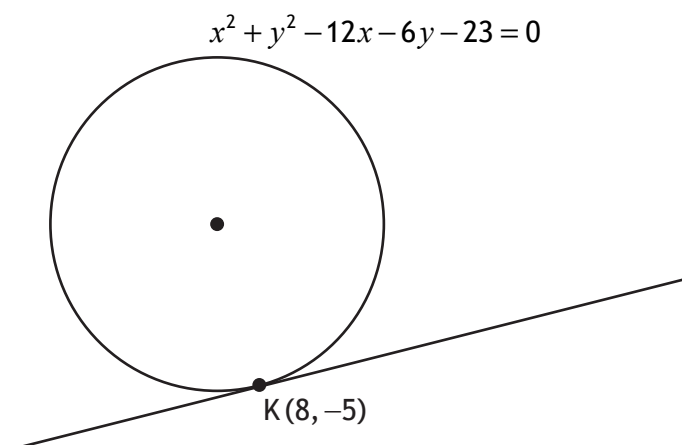
3

3. Given $h(x) = 3\cos 2x$, find the value of $h'\left(\frac{\pi}{6}\right)$.

3

[Turn over

4. The point $K(8, -5)$ lies on the circle with equation $x^2 + y^2 - 12x - 6y - 23 = 0$.



Find the equation of the tangent to the circle at K .

4

5. $A(-3, 4, -7)$, $B(5, t, 5)$ and $C(7, 9, 8)$ are collinear.

(a) State the ratio in which B divides AC .

1

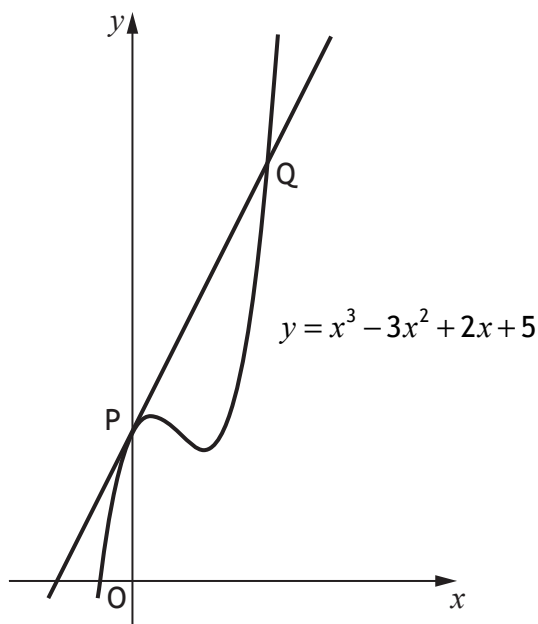
(b) State the value of t .

1

6. Find the value of $\log_5 250 - \frac{1}{3} \log_5 8$.

3

7. The curve with equation $y = x^3 - 3x^2 + 2x + 5$ is shown on the diagram.

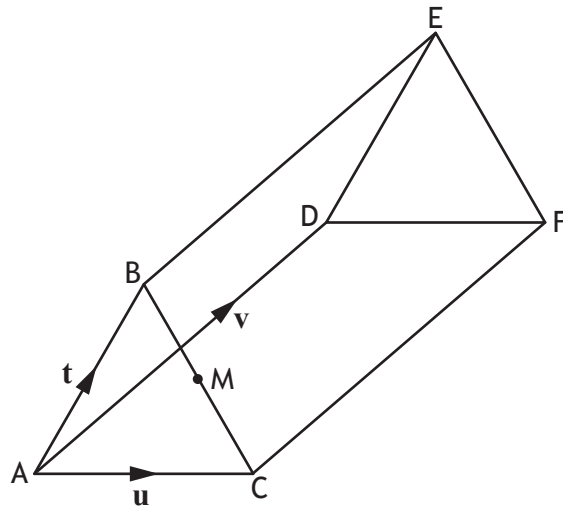


- | | |
|--|---|
| (a) Write down the coordinates of P, the point where the curve crosses the y -axis . | 1 |
| (b) Determine the equation of the tangent to the curve at P. | 3 |
| (c) Find the coordinates of Q, the point where this tangent meets the curve again. | 4 |
8. A line has equation $y - \sqrt{3}x + 5 = 0$.
Determine the angle this line makes with the positive direction of the x -axis.
- 2

[Turn over

9. The diagram shows a triangular prism ABC,DEF.

$\vec{AB} = \mathbf{t}$, $\vec{AC} = \mathbf{u}$ and $\vec{AD} = \mathbf{v}$.



- (a) Express $\vec{BC}$ in terms of $\mathbf{u}$ and $\mathbf{t}$.

1

M is the midpoint of BC.

- (b) Express $\vec{MD}$ in terms of $\mathbf{t}$, $\mathbf{u}$ and $\mathbf{v}$.

2

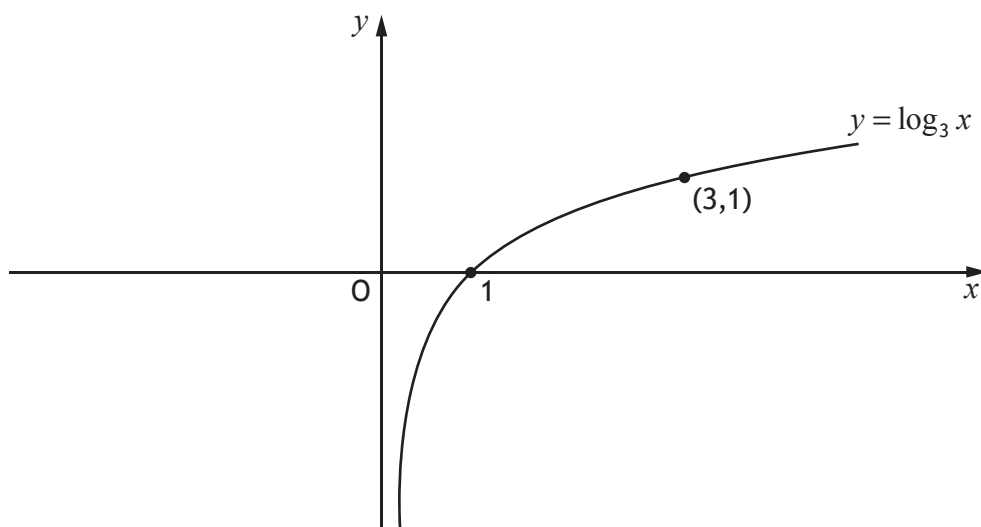
10. Given that

- $\frac{dy}{dx} = 6x^2 - 3x + 4$, and
- $y = 14$ when $x = 2$,

express y in terms of x .

4

11. The diagram shows the curve with equation $y = \log_3 x$.



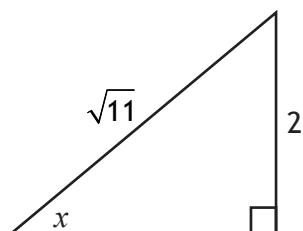
- (a) On the diagram in your answer booklet, sketch the curve with equation $y = 1 - \log_3 x$. 2
- (b) Determine the exact value of the x -coordinate of the point of intersection of the two curves. 3

12. Vectors $\mathbf{a}$ and $\mathbf{b}$ are such that $\mathbf{a} = 4\mathbf{i} - 2\mathbf{j} + 2\mathbf{k}$ and $\mathbf{b} = -2\mathbf{i} + \mathbf{j} + p\mathbf{k}$.

- (a) Express $2\mathbf{a} + \mathbf{b}$ in component form. 1
- (b) Hence find the values of p for which $|2\mathbf{a} + \mathbf{b}| = 7$. 3

[Turn over for next question]

13. The right-angled triangle in the diagram is such that $\sin x = \frac{2}{\sqrt{11}}$ and $0 < x < \frac{\pi}{4}$.



(a) Find the exact value of:

(i) $\sin 2x$

3

(ii) $\cos 2x$.

1

(b) By expressing $\sin 3x$ as $\sin(2x + x)$, find the exact value of $\sin 3x$.

3

14. Evaluate $\int_{-4}^9 \frac{1}{\sqrt[3]{(2x+9)^2}} dx$.

5

15. A cubic function, f , is defined on the set of real numbers.

- $(x+4)$ is a factor of $f(x)$
- $x=2$ is a repeated root of $f(x)$
- $f'(-2) = 0$
- $f'(x) > 0$ where the graph with equation $y = f(x)$ crosses the y -axis

Sketch a possible graph of $y = f(x)$ on the diagram in your answer booklet.

4

[END OF QUESTION PAPER]