

Paper 2

Question		Generic Scheme	Illustrative Scheme	Max Mark
1	a			
• ¹	ss	find gradient of AB	• ¹ $m_{AB} = 1$	4
• ²	pd	find perpendicular gradient	• ² $m_{perp} = -1$ stated or implied by • ⁴	
• ³	pd	find midpoint of AB	• ³ (4,1) stated or implied by • ⁴	
• ⁴	pd	obtain equation	• ⁴ $y - 1 = -1(x - 4)$	

Notes:

- ⁴ is only available as a consequence of using a perpendicular gradient **and** a midpoint.
- The gradient must appear in simplified form at •⁴ stage for •⁴ to be awarded.

Commonly Observed Responses:

Candidate A

$$m_{AB} = -1 \quad \bullet^1 \text{ X}$$

$$m_{perp} = 1 \quad \bullet^2 \text{ ✓}$$

$$(4,1) \quad \bullet^3 \text{ ✓}$$

$$y - 1 = 1(x - 4) \Rightarrow y = x - 3 \quad \bullet^4 \text{ ✓}$$

Leading to part (b)

$$y - x = -3 \quad \bullet^5 \text{ ✓}$$

$$y + 2x = 6 \quad \bullet^6 \text{ ✓}$$

$$(3,0) \quad \bullet^6 \text{ ✓}$$

•⁷ and •⁸ are not available as $A = T = (3,0)$

Question		Generic Scheme	Illustrative Scheme	Max Mark
1	b			
• ⁵	ss	know to solve simultaneously	• ⁵ $y + 2x = 6$ $y + x = 5$	2
• ⁶	pd	solve correctly for x and y	• ⁶ $x = 1, y = 4$	

Commonly Observed Responses:

Candidate B

Part (a) $y - 1 = -1(x - 4)$ •⁴ ✓
 $y = -x + 3$ error

Part (b) $y + 2x = 6$ and $y + x = 3$ •⁵ ✓
 $x = 3, y = 0$ •⁶ ✗ correct strategy used, pd mark not available

1	c			
• ⁷	ss	know and use $m = \tan \theta$	• ⁷ $\tan \theta = -2$	2
• ⁸	pd	calculate angle	• ⁸ 116.6° accept 117° or 2.03 radians	

Commonly Observed Responses:

Candidate C

$m_{AT} = -\frac{1}{2}$
base angle = 26.6° •⁷ ✗
 \Rightarrow angle = $90 + 26.6 = 116.6^\circ$ •⁸ ✗

Candidate D

$m_{AT} = 2$ •⁷ ✗
angle = $\tan^{-1}(2) = 63.4^\circ$ •⁸ ✓

Candidate E:

Part (a)

$m_{AB} = \frac{2-0}{5-3} = \frac{2}{8} = \frac{1}{4}$ •¹ ✗

$m_{\text{perp}} = -4$ •² ✓

Midpoint of AB (4, 1) •³ ✓

$y - 1 = -4(x - 1)$ •⁴ ✓

$y + 4x - 5$

Part (b)

$y + 4x - 5 = 0$ •⁵ ✗ \Rightarrow $y + 2x = -6$ •⁶ ✗
 $y + 2x + 6 = 0$

$\Rightarrow 2x = 1, x = \frac{1}{2}, y = -7$

•⁵ is a strategy mark. The correct strategy is to solve the **given equation** with the equation from part (a) simultaneously. •⁵ is not awarded as the given equation has not been used.

The equation obtained at stage •⁴, has been rearranged incorrectly in part (b). The next pd mark, •⁶, is therefore not awarded.

Question	Generic Scheme	Illustrative Scheme	Max Mark
2			
• ¹ ss	know to and differentiate	• ¹ $4x^3 - 6x^2$	4
• ² ic	find gradient	• ² 8	
• ³ pd	find y -coordinate	• ³ 5	
• ⁴ ic	state equation of tangent	• ⁴ $y - 5 = 8(x - 2)$	

Notes:

1. •⁴ is only available if an attempt has been made to find the gradient from differentiation **and** calculating the y -coordinate by substitution into the original equation.

Commonly Observed Responses:

Candidate A

•¹ ✓ •² ✓ •³ ✓

using $y = mx + c$

$x = 2, y = 5, m = 8$

$\Rightarrow 5 = 8 \times 2 + c$

$\Rightarrow c = -11$ •⁴ ✓

$y = 8x - 11$

Question		Generic Scheme	Illustrative Scheme	Max Mark
3	a			
• ¹	ic	interpret notation	• ¹ $f(x+3)$ stated or implied by • ²	2
• ²	pd	a correct expression	• ² $= (x+3)(x+2)+q$ OR $= (x+3)^2 - (x+3) + q$ or equivalent	
Notes:				
1. Special Case: • ¹ is for substituting $(x+3)$ for x thus, treat $x+3(x+3-1)+q$ as bad form.				
Commonly Observed Responses:				
Candidate A		Candidate B		
$f(g(x)) = x+3(x+3-1)+q$ • ¹ ✓ $= x^2+5x+6+q$ • ² ✓ • ³ ✓		$f(g(x)) = x+3(x+3-1)+q$ • ¹ ✓ $= 4x+6+q$ • ² ✗		
Candidate C		Candidate D		
$f(g(x)) = x+3(x+3-1)+q$ • ¹ ✓ $= (x+3)^2 - x + 3 + q$ $x^2+5x+6+q=0$ • ² ✓ • ³ ✓		$f(g(x)) = (x+3)(x+3-1)+q$ • ¹ ✓ • ² ✓ $= (x+3)^2 - x + 3 + q$ $x^2+5x+12+q=0$ • ³ ✗		
Candidate E: using $g(f(x))$				
part (a)		part (b)		
$g(f(x)) = g(x(x-1)+q)$ • ¹ ✗ $= x(x-1)+q+3$ • ² ✓		$x^2 - x + q + 3 = 0$ • ³ ✗ (eased) $b^2 - 4ac = (-1)^2 - 4 \times 1 \times (q+3)$ • ⁴ ✓ $1 - 4q - 12 = 0$ • ⁵ ✓ $q = -\frac{11}{4}$ • ⁶ ✓		
Leading to				

Question		Generic Scheme	Illustrative Scheme	Max Mark
3	b			
• ³	pd	Method 1 write in standard quadratic form	• ³ $x^2 + 5x + 6 + q = 0$	4
• ⁴	ic	use discriminant	• ⁴ $b^2 - 4ac = 5^2 - 4 \times 1 \times (6 + q)$	
• ⁵	pd	simplify and equate to zero	• ⁵ $\Rightarrow 25 - 24 - 4q = 0$	
• ⁶	pd	find value of q	• ⁶ $q = \frac{1}{4}$	
• ³	pd	Method 2 write in standard quadratic form	• ³ $x^2 + 5x + 6 + q = 0$	
• ⁴	ic	complete the square	• ⁴ $\left(x + \frac{5}{2}\right)^2 - \frac{25}{4} + 6 + q = 0$	
• ⁵	pd	equate to zero	• ⁵ $-\frac{25}{4} + 6 + q = 0$	
• ⁶	pd	find value of q	• ⁶ $q = \frac{1}{4}$	
• ³	pd	Method 3 write in standard quadratic form	• ³ $f(g(x)) = x^2 + 5x + 6 + q = 0$	
• ⁴	ic	geometric interpretation	• ⁴ equal roots so touches x -axis at SP	
• ⁵	pd	differentiates to obtain x	• ⁵ $\Rightarrow \frac{dy}{dx} = 2x + 5 = 0$ $x = -\frac{5}{2}$	
• ⁶	pd	find value of q	• ⁶ $\frac{25}{4} - \frac{25}{2} + 6 + q = 0$ $q = \frac{1}{4}$	

Notes:

- Do not penalise the omission of ' $= 0$ ' at •³.
- In Method 1 $a=1$, $b=5$, $c=6+q$ is sufficient for •³.
- Candidates who assume ' $= 0$ ' and follow through to a correct value of q , •⁶ is still available. In Methods 1 and 2 ' $= 0$ ' must appear at •⁴ or •⁵ for •⁵ to be awarded.
- If the expression obtained at •³ is not a quadratic then •³, •⁴, •⁵ and •⁶ are not available.

Question	Generic Scheme	Illustrative Scheme	Max Mark
Throughout this question treat coordinates written as components, and vice versa, as bad form.			
4	a		
• ¹	pd	states coordinates of C	• ¹ C(11,12,6)
• ²	pd	states coordinates of D	• ² D(8,8,4)
Notes:			
<p>1. Accept $x=11$, $y=12$ and $z=6$ for •¹ and $x=8$, $y=8$ and $z=4$ for •².</p> <p>2. For candidates who write the coordinates as Cartesian triples and omit brackets in both cases, •² is not available.</p>			
4	b		
• ³	pd	finds \overrightarrow{CB}	• ³ $\begin{pmatrix} 0 \\ -8 \\ -4 \end{pmatrix}$
• ⁴	pd	finds \overrightarrow{CD}	• ⁴ $\begin{pmatrix} -3 \\ -4 \\ -2 \end{pmatrix}$
Notes:			
3. For candidates who find both \overrightarrow{BC} and \overrightarrow{DC} , only • ⁴ is available (repeated error).			
4	c	.	
• ⁵	ss	know to use scalar product applied to the correct angle	• ⁵ $\cos \hat{BCD} = \frac{\overrightarrow{CB} \cdot \overrightarrow{CD}}{ \overrightarrow{CB} \overrightarrow{CD} }$
• ⁶	pd	find scalar product	• ⁶ 40
• ⁷	pd	find $ \overrightarrow{CB} $	• ⁷ $\sqrt{80}$
• ⁸	pd	find $ \overrightarrow{CD} $	• ⁸ $\sqrt{29}$
• ⁹	pd	find angle	• ⁹ 33.9°
Notes:			
<p>4. •⁵ is not available for candidates who choose to evaluate an incorrect angle.</p> <p>5. •⁹ accept 33.8 to 34 degrees or 0.59 to 0.6 radians.</p> <p>6. If candidates do not attempt •⁹, then •⁵ is only available if the formula quoted relates to the labelling in the question.</p> <p>7. •⁹ is only available as a result of using a valid strategy.</p> <p>8. •⁵ is not available for candidates who write $\cos \theta = \frac{40}{\sqrt{80} \times \sqrt{29}}$. Some reference to the labelling of the diagram must be made within their solution to part (c), to indicate they are attempting to find the correct angle.</p>			

Commonly Observed Responses:

<p>Candidate A: Cosine Rule</p> $\cos \hat{B}CD = \frac{CB^2 + CD^2 - BD^2}{2 \times CB \times CD} \quad \bullet^5 \checkmark$ $CB = \sqrt{80}, CD = \sqrt{29}, BD = \sqrt{29} \quad \bullet^6 \checkmark \bullet^7 \checkmark \bullet^8 \checkmark$ \checkmark $33.9^\circ \text{ or } 0.59 \text{ radians} \quad \bullet^9 \checkmark$	<p>Candidate B</p> $\cos \hat{B}CD = \frac{\overline{BC} \cdot \overline{CD}}{ \overline{BC} \times \overline{CD} } \quad \bullet^5 \times$ $\overline{BC} \cdot \overline{CD} = -40 \quad \bullet^6 \times$ $ \overline{BC} = \sqrt{80}, \overline{CD} = \sqrt{29} \quad \bullet^7 \times \bullet^8 \times$ $146.1^\circ \text{ or } 2.55 \text{ radians} \quad \bullet^9 \checkmark$
<p>Candidate C</p> $\cos \hat{B}OD = \frac{\overline{OB} \cdot \overline{OD}}{ \overline{OB} \times \overline{OD} } \quad \bullet^5 \times$ $\overline{OB} \cdot \overline{OD} = 128 \quad \bullet^6 \checkmark$ $ \overline{OB} = \sqrt{141}, \overline{OD} = 12 \quad \bullet^7 \checkmark \bullet^8 \checkmark$ $26.1^\circ \text{ or } 0.46 \text{ radians} \quad \bullet^9 \checkmark$	<p>Candidate D</p> $\cos \hat{C}BD = \frac{\overline{BC} \cdot \overline{BD}}{ \overline{BC} \times \overline{BD} } \quad \bullet^5 \times$ $\overline{BC} \cdot \overline{BD} = 40 \quad \bullet^6 \checkmark$ $ \overline{BC} = \sqrt{80}, \overline{BD} = \sqrt{29} \quad \bullet^7 \checkmark \bullet^8 \checkmark$ $33.9^\circ \text{ or } 0.59 \text{ radians} \quad \bullet^9 \checkmark$
<p>Candidate E</p> $\cos \hat{B}OC = \frac{\overline{OB} \cdot \overline{OC}}{ \overline{OB} \times \overline{OC} } \quad \bullet^5 \times$ $\overline{OB} \cdot \overline{OC} = 181 \quad \bullet^6 \checkmark$ $ \overline{OB} = \sqrt{141}, \overline{OC} = \sqrt{301} \quad \bullet^7 \checkmark \bullet^8 \checkmark$ $28.5^\circ \text{ or } 0.50 \text{ radians} \quad \bullet^9 \checkmark$	<p>Candidate F</p> $\cos \hat{B}CD = \frac{\overline{BC} \cdot \overline{DC}}{ \overline{BC} \times \overline{DC} } \quad \bullet^5 \checkmark$ <p>this is an acceptable form for the scalar product.</p>

Question	Generic Scheme	Illustrative Scheme	Max Mark
5			
• ¹ ss	start to integrate	• ¹ $\frac{1}{\frac{1}{2}}(\dots)^{\frac{1}{2}}$	
• ² pd	complete integration	• ² $\dots \times \frac{1}{3}$	
• ³ pd	process limits	• ³ $\frac{2}{3}(3t+4)^{\frac{1}{2}} - \frac{2}{3}(3(4)+4)^{\frac{1}{2}}$	
• ⁴ pd	start to solve equation	• ⁴ $(3t+4)^{\frac{1}{2}} = 7$	
• ⁵ pd	solve for t	• ⁵ $t = 15$	5

Notes:

- ³ is awarded for correct substitution leading to $F(t) - F(4)$ where $F(x)$ is the candidates attempt
- to integrate $(3x+4)^{-\frac{1}{2}}$. For substituting into the original function •³ is unavailable.
- ⁵ is only available as a consequence of squaring both sides of an equation.
- The integral obtained must contain a non integer power for •⁴ and •⁵ to be available.
- Do not penalise the inclusion of '+c'.
- Incorrect expansion of $(\dots)^{-\frac{1}{2}}$ at stage •¹, only •³ is available as follow through. Incorrect expansion of $(\dots)^{\frac{1}{2}}$ at stage •⁴, •⁴ and •⁵ are not available.

Commonly Observed Responses:

<p>Candidate A: Forgetting the $\frac{1}{3}$</p> $\left[2(3x+4)^{\frac{1}{2}} \right]_4^t = 2 \quad \bullet^1 \checkmark \quad \bullet^2 \times$ $\left(2(3t+4)^{\frac{1}{2}} \right) - \left(2(3(4)+4)^{\frac{1}{2}} \right) = 2 \quad \bullet^3 \checkmark$ $(3t+4)^{\frac{1}{2}} = 5 \quad \bullet^4 \checkmark$ $t = 7 \quad \bullet^5 \checkmark$	<p>Candidate B</p> $\left[\frac{1}{6}(3x+4)^{\frac{1}{2}} \right]_4^t = 2 \quad \bullet^1 \times \quad \bullet^2 \checkmark$ $\left(\frac{1}{6}(3t+4)^{\frac{1}{2}} \right) - \left(\frac{1}{6}(3(4)+4)^{\frac{1}{2}} \right) = 2 \quad \bullet^3 \checkmark$ $(3t+4)^{\frac{1}{2}} = 16 \quad \bullet^4 \checkmark$ $t = 84 \quad \bullet^5 \checkmark$
<p>Candidate C</p> $\left[\frac{(3x+4)^{\frac{1}{2}}}{\frac{1}{2}} \times 3 \right]_4^t = 2 \quad \bullet^1 \checkmark \quad \bullet^2 \times$ $\left[\frac{2}{3}(3x+4)^{\frac{1}{2}} \right]_4^t = 2$ $\left[\frac{2}{3}(3t+4)^{\frac{1}{2}} \right] - \left[\frac{2}{3}(3(4)+4)^{\frac{1}{2}} \right] = 2 \quad \bullet^3 \times$ $(3t+4)^{\frac{1}{2}} = 7 \quad \bullet^4 \checkmark$ $t = 15 \quad \bullet^5 \checkmark$	<p>Candidate D</p> $\left[-\frac{3}{2}(3x+4)^{-\frac{3}{2}} \right]_4^t = 2 \quad \bullet^1 \times \quad \bullet^2 \times$ $-\frac{3}{2}(3t+4)^{-\frac{3}{2}} - \left(-\frac{3}{2} \times 16^{-\frac{3}{2}} \right) = 2 \quad \bullet^3 \checkmark$ $(3t+4)^{\frac{3}{2}} = -\frac{192}{253} \quad \bullet^4 \checkmark$ <p>decimal equivalent not accepted</p> $t = -1.056 \quad \bullet^5 \checkmark$

Question	Generic Scheme	Illustrative Scheme	Max Mark
6			
	<ul style="list-style-type: none"> •¹ ss use correct double angle formula •² ss arrange in standard quadratic form •³ ss start to solve •⁴ ic reduce to equations in $\sin x$ only •⁵ pd process to find solutions in given domain 	<ul style="list-style-type: none"> •¹ $\sin x - 2(1 - 2\sin^2 x)$ stated or implied by •² •² $4\sin^2 x + \sin x - 3 = 0$ •³ $(4\sin x - 3)(\sin x + 1) = 0$ <li style="text-align: center;">OR $\frac{-1 \pm \sqrt{(1)^2 - 4 \times 4 \times (-3)}}{2 \times 4}$ •⁴ $\sin x = \frac{3}{4}$ and $\sin x = -1$ •⁵ $0.848, 2.29$ and $\frac{3\pi}{2}$ <li style="text-align: center;">OR •⁴ $\sin x = \frac{3}{4}$ and $x = 0.848, 2.29$ •⁵ $\sin x = -1$, and $x = \frac{3\pi}{2}$ 	5

Notes:

1. •¹ is not available for simply stating $\cos 2A = 1 - 2\sin^2 A$ with no further working.
2. In the event of $\cos^2 x - \sin^2 x$ or $2\cos^2 x - 1$ being substituted for $\cos 2x$, •¹ cannot be awarded until the equation reduces to a quadratic in $\sin x$.
3. Substituting $1 - 2\sin^2 A$ or $1 - 2\sin^2 \alpha$ for $\cos 2\alpha$ at •¹ stage should be treated as bad form provided the equation is written in terms of x at stage •². Otherwise, •¹ is not available.
4. ‘=0’ must appear by •³ stage for •² to be awarded. However, for candidates using the quadratic formula to solve the equation, ‘=0’ must appear at •² stage for •² to be awarded.
5. Candidates may express the equation obtained at •² in the form $4s^2 + s - 3 = 0$ or $4x^2 + x - 3 = 0$. In these cases, award •³ for $(4s - 3)(s + 1) = 0$ or $(4x - 3)(x + 1) = 0$. However, •⁴ is only available if $\sin x$ appears explicitly at this stage.
6. •⁴ and •⁵ are only available as a consequence of solving a quadratic equation.
7. •³, •⁴ and •⁵ are not available for any attempt to solve a quadratic written in the form $ax^2 + bx = c$.
8. •⁵ is not available to candidates who work in degrees and do not convert their solutions into radian measure.
9. $\sin x + 4\sin^2 x - 3 = 0$ does not gain •², unless •³ is awarded.

Commonly Observed Responses:

Commonly Observed Responses:	
<p>Candidate A</p> <p>•¹ ✓ •² ✓ $(4s-3)(s+1)=0$ $s = \frac{3}{4}, s = -1$ $x = 0.848, 2.29$ and $\frac{3\pi}{2}$</p>	<p>•³ ✓ •⁴ ✗ •⁵ ✓</p>
<p>Candidate B</p> <p>•¹ ✓ $4\sin^2 x + \sin x - 3 = 0$ $5\sin x - 3 = 0$ $\sin x = \frac{3}{5}$ $x = 0.644, 2.50$</p>	<p>•² ✓ •³ ✗ •⁴ ✗ •⁵ ✗</p>
<p>Candidate C</p> <p>•¹ ✓ $\sin x - 2(1 - 2\sin^2 x) = 1$ $\sin x - 2 + 4\sin^2 x = 1$ $4\sin^2 x + \sin x = 3$ $\sin x(4\sin x + 1) = 3$ $\sin x = 3, 4\sin x + 1 = 3$ no solution, $\sin x = \frac{1}{2}$ $x = \frac{\pi}{6}, \frac{5\pi}{6}$</p>	<p>•² ✗ •³ ✗ •⁴ ✗ •⁵ ✗</p>
<p>Candidate D</p> <p>•¹ ✓ $\sin x - 2(1 - 2\sin^2 x) = 1$ $4\sin^2 x + \sin x - 3 = 0$ $4\sin^2 x + \sin x = 3$ $\sin x(4\sin x + 1) = 3$ $\sin x = 3, 4\sin x + 1 = 3$ no solution, $\sin x = \frac{1}{2}$ $x = \frac{\pi}{6}, \frac{5\pi}{6}$</p>	<p>•² ✓ •³ ✗ •⁴ ✗ •⁵ ✗</p>
<p>Candidate E: Reading $\cos 2x$ as $\cos^2 x$</p> <p>$\sin x - 2\cos^2 x = 1$ •¹ ✗ $\sin x - 2(1 - \sin^2 x) = 1$ $2\sin^2 x + \sin x - 3 = 0$ •² ✗ $(2\sin x + 3)(\sin x - 1) = 0$ •³ ✗ $\sin x = -\frac{3}{2}, \sin x = 1$ •⁴ ✗ no solution, $x = \frac{\pi}{2}$ •⁵ ✗</p>	

Question		Generic Scheme	Illustrative Scheme	Max Mark
7	a			
• ¹	ss	know to and find intersection of line and curve	• ¹ $2x = 6x - x^2 \Rightarrow x = 0, x = 4$	
• ²	ic	use “upper – lower”	• ² $\int((6x - x^2) - 2x) dx$	
• ³	pd	integrate	• ³ $2x^2 - \frac{1}{3}x^3$	
• ⁴	pd	substitute limits and evaluate	• ⁴ $10\frac{2}{3}$	
• ⁵	pd	evaluate area developed	• ⁵ $10\frac{2}{3} \times 300 = 3200 \text{m}^2$	5
Notes:				
<p>1. ‘0’ appearing as the lower limit of the integral is sufficient evidence for $x = 0$ at •¹ stage.</p> <p>2. •⁵ is only available as a consequence of multiplying an exact answer at •⁴ stage.</p> <p>3. The omission of dx at •² should not be penalised.</p> <p>4. Where a candidate differentiates one or both terms •³, •⁴ and •⁵ are unavailable.</p> <p>5. Do not penalise the inclusion of ‘+ c’.</p> <p>6. Accept $\int(4x - x^2) dx$ for •².</p>				

Commonly Observed Responses:

Candidate A

$$\int_0^4 (2x - (6x - x^2)) dx \quad \bullet^2 \text{ X}$$

$$= \frac{1}{3}x^3 - 2x^2 \quad \bullet^3 \text{ ✓}$$

$$= -10\frac{2}{3} \text{ cannot be negative so } = 10\frac{2}{3} \quad \bullet^4 \text{ X} \quad \text{however } \dots = -10\frac{2}{3} \text{ so Area } = 10\frac{2}{3} \quad \bullet^4 \text{ ✓}$$

$$\text{Area} = 3200\text{m}^2 \quad \bullet^5 \text{ ✓}$$

Candidate B

$$2x = 6x - x^2 \Rightarrow x = 0, 4 \quad \bullet^1 \text{ ✓}$$

Shaded area

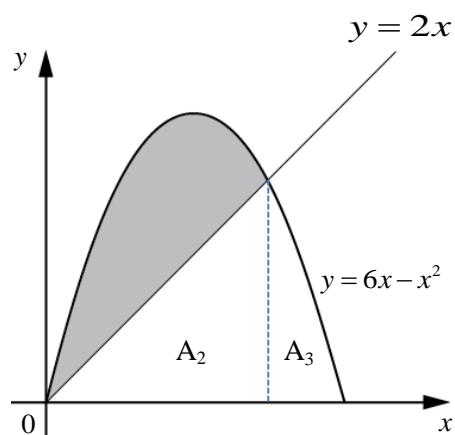
$$= \text{area under parabola} - (A_2 + A_3)$$

$$= \int_0^6 (6x - x^2) dx - \left[A_2 + \int_4^6 (6x - x^2) dx \right] \quad \bullet^2 \text{ ✓}$$

Stated or implied by \bullet^4

$$\text{Area under parabola} = 36, A_2 = 16 \text{ and } A_3 = \frac{28}{3} \quad \bullet^3 \text{ ✓}$$

$$\text{Shaded area} = 36 - \left(16 + \frac{28}{3} \right) = \frac{32}{3} \quad \bullet^4 \text{ ✓}$$



Candidate C

Part (a)

$$x = 0, x = 6 \quad \bullet^1 \text{ X}$$

$$\int ((6x - x^2) - 2x) dx \quad \bullet^2 \text{ ✓}$$

$$\left[2x^2 - \frac{1}{3}x^3 \right]_0^6 \quad \bullet^3 \text{ ✓}$$

$$\left(2 \times 6^2 - \frac{1}{3} \times 6^3 \right) - (0) = 0 \quad \bullet^4 \text{ X}$$

$$\Rightarrow \text{Area} = 0 \times 300 = 0 \text{ m}^2 \quad \bullet^5 \text{ ✓}$$

Question		Generic Scheme	Illustrative Scheme	Max Mark
7	b			
• ⁶	ss	set derivative to 2	• ⁶ $6 - 2x = 2$	5
• ⁷	pd	find point of contact	• ⁷ $x = 2, y = 8$	
• ⁸	pd	find equation of road	• ⁸ $y = 2x + 4$	
• ⁹	ss	find correct integral	• ⁹ $\left[(x^2 + 4x) - \left(3x^2 - \frac{1}{3}x^3 \right) \right]_0^2$	
• ¹⁰	ic	calculate area	• ¹⁰ 800m^2	

Notes:

6. For candidates who omit 'm²' at both •⁵ and •¹⁰ stages, •¹⁰ is not available.
7. Candidates who arrive at an incorrect equation at •⁸, or produce an equation ex nihilo, must use an equation of the form $y = 2x + c$ with $c > 0$, for •⁹ and •¹⁰ to be available.
8. $y = 2x + 4$ must appear explicitly or as part of the integrand for •⁸ to be awarded.
9. •¹⁰ is only available as a result of a valid strategy at the •⁹ stage,
ie $\int (\text{line}) - (\text{quadratic})$ **and** lower limit = 0 and upper limit < 3.

Commonly Observed Responses:

Candidate D: Alternative Method

Line has equation of the form $y = 2x + c$, $y = 2x + c$ and $y = 6x - x^2$

intersect where $x^2 - 4x + c = 0$

•⁶ ✓

tangency \Rightarrow 1 point of intersection

$$\Rightarrow b^2 - 4ac = 0$$

•⁷ ✓

$$16 - 4c = 0$$

•⁸ ✓

$$c = 4$$

Continue as above.

Question	Generic Scheme		Illustrative Scheme	Max Mark
8				
• ¹	pd	correct values	• ¹ $g = -p, f = -2p, c = 3p + 2$	5
• ²	ss	substitute and rearrange	• ² $5p^2 - 3p - 2$	
• ³	ic	knowing condition	• ³ $g^2 + f^2 - c > 0$	
• ⁴	pd	factorise and solve	• ⁴ $(5p + 2)(p - 1) = 0 \Rightarrow p = -\frac{2}{5}, p = 1$	
• ⁵	ic	correct range	• ⁵ $p < -\frac{2}{5}, p > 1$	

Notes:

- Candidates who state the coordinates of the centre, $(p, 2p)$ and state the radius, $r = \sqrt{\dots - (3p + 2)}$ gain •¹.
- Accept $(-p)^2 + (-2p)^2 - (3p + 2)$ or $p^2 + (2p)^2 - (3p + 2)$. If brackets are omitted •¹ may only be awarded if subsequent working is correct.
- Do not accept $(-p)^2 + (2p)^2 - (3p + 2)$ or $(p)^2 + (-2p)^2 - (3p + 2)$ for •¹.
- Do not accept $g^2 + f^2 - c \geq 0$ for •³.
- For a candidate who uses $c = 2$ and follows through to get $p < -\sqrt{\frac{2}{5}}, p > \sqrt{\frac{2}{5}}$, award •², •³ and •⁵.
- Evidence for •³ may appear at •⁵ stage.
- ⁴ and •⁵ can only be awarded for solving a quadratic inequation.

Commonly Observed Responses:

Candidate A	Candidate B
$g = -2p, f = -4p, c = 3p + 2$	$(x - p)^2 - p^2 + (y - 2p)^2 - 4p^2 + 3p + 2 = 0$
$20p^2 - 3p - 2$	$(x - p)^2 + (y - 2p)^2$
$g^2 + f^2 - c > 0$	$= 5p^2 - 3p - 2$
$(4p + 1)(5p - 2) = 0 \Rightarrow p = -\frac{1}{4}, p = \frac{2}{5}$	$5p^2 - 3p - 2 > 0$
$p < -\frac{1}{4}, p > \frac{2}{5}$	$(5p + 2)(p - 1) > 0$
	$p < -\frac{2}{5}, p > 1$

Question		Generic Scheme	Illustrative Scheme	Max Mark
9	a			
• ¹	ss	know to differentiate	• ¹ $a = v'(t)$	3
• ²	pd	differentiates trig. function	• ² $-8\sin\left(2t - \frac{\pi}{2}\right) \dots\dots$	
• ³	pd	applies chain rule	• ³ $\dots\dots \times 2$ and complete $a(t) = -16\sin\left(2t - \frac{\pi}{2}\right)$	

Commonly Observed Responses:

Candidate A: Alternative Method

Part (a)

$$v(t) = 8\cos\left(2t - \frac{\pi}{2}\right) = 8\sin 2t$$

$$v'(t) = \dots \quad \bullet^1 \checkmark$$

$$= 8\cos 2t \dots$$

$$\bullet^2 \checkmark$$

$$= \dots \times 2 \quad \bullet^3 \checkmark$$

Part (b)

$$v'(10) = 16\cos 20 = 6.53 \quad \bullet^4 \checkmark$$

$> 0, \Rightarrow$ velocity is increasing $\bullet^5 \checkmark$

Part (c)

$$s(t) = \int v(t) dt \quad \bullet^6 \checkmark$$

$$s(t) = -4\cos 2t + c \quad \bullet^7 \checkmark$$

$$4 = -4 + c \Rightarrow c = 8$$

$$\Rightarrow s(t) = -4\cos 2t + 8 \quad \bullet^8 \checkmark$$

$$\text{or } \Rightarrow s(t) = 8 - 4\cos 2t$$

Candidate B: Candidates who misinterpret the process for rate of change.

Part (a)

$$a(t) = \int 8\cos\left(2t - \frac{\pi}{2}\right) dt$$

$$= 4\sin\left(2t - \frac{\pi}{2}\right) + c$$

Wrong process award $\frac{0}{3}$

Part (b)

$$\text{If } t = 10, a = 4\sin\left(20 - \frac{\pi}{2}\right) + c$$

$$= -1.63 + c$$

Cannot evaluate award $\frac{0}{2}$

Part (c)

$$s = v'(t)$$

$$s(t) = -16\sin\left(2t - \frac{\pi}{2}\right)$$

Award $\frac{2}{3}$

Candidate C

Part (a)

$$a = v'(t) \text{ or equivalent} \quad \bullet^1$$

$$a = 4\sin\left(2t - \frac{\pi}{2}\right) \quad \bullet^2 \times \quad \bullet^3 \times$$

Part (b)

$$a(10) = 4\sin\left(20 - \frac{\pi}{2}\right) = -1.63 \quad \bullet^4$$

< 0 , So decreasing $\bullet^5 \checkmark$

Only as a consequence of \bullet^1 in part (a)

Question		Generic Scheme	Illustrative Scheme	Max Mark
9	b			
• ⁴	ss	know to and evaluate $a(10)$	• ⁴ $a(10) = 6.53$	2
• ⁵	ic	interpret result	• ⁵ $a(10) > 0$ therefore increasing	

Notes:

- ⁵ is available only as a consequence of substituting into a derivative.
- ⁴ and •⁵ are not available to candidates who work in degrees.
- ² and •³ may be awarded if they appear in the working for 9(b). However, •¹ requires a clear link between acceleration and $v'(t)$.

9	c			
• ⁶	ic	know to integrate	• ⁶ $s(t) = \int v(t) dt$	3
• ⁷	pd	integrate correctly	• ⁷ $s(t) = 4 \sin\left(2t - \frac{\pi}{2}\right) + c$	
• ⁸	ic	determine constant and complete	• ⁸ $c = 8$ so $s(t) = 4 \sin\left(2t - \frac{\pi}{2}\right) + 8$	

Notes:

- ⁷ and •⁸ are not available to candidates who work in degrees. However, accept $\int 8 \cos(2t - 90) dt$ for •⁶.

[END OF MARKING INSTRUCTIONS]